## BABCOCK UNIVERSITY



CENTRE FOR OPEN DISTANCE AND ELEARNING (BUCODeL)

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## AUTHENTIC ASSESSMENT

COURSE CODE: ..... BSAD 112
COURSE TITTLE: BUSINESS MATHEMATICS II
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## TOPIC: FUNCTIONS OF REAL VARIABLES

## LEARNING OUTCOMES:

At the end of this topic, learners are expected to:

1. Recognize real numbers
2. Analyze various types of functions.
3. Solve problems relating to composite functions
4. Substitute for each function to obtain total score.

Assessment Description (Task) (6 marks)
Suppose the cost of manufacturing $q$ units of a certain commodity is given as a function $C(q)=q^{3}-30 q^{2}+500 q+200$.
What is the cost of manufacturing 10 units of commodity? (6marks)

## GRADING RUBRICS

|  | REALISTIC OBJECTIVES | POOR | EXCELLENT |
| ---: | :--- | :--- | :--- |
| 1. | Identify the value for q | Not <br> identifying <br> the values <br> for q <br> $\mathbf{0}$ mark | Proper <br> identification of <br> the value for q |
| 2. | Substitute correctly the values of q | Not <br> substituting <br> the correct <br> values of q | Substitute correctly <br> the values of q |
| 3. | Put the powers into consideration in the <br> function | The powers <br> are not <br> properly put <br> into | The powers are put <br> into consideration <br> in the cost function |


|  |  | consideration <br> in the cost <br> function |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{0}$ mark | $\mathbf{2}$ marks |  |  |
| 4. | Final answer for the task | Incorrect <br> final answer <br> to the task <br> $\mathbf{0}$ mark | Correct final <br> answer to the task |

## TOPIC: LIMITS OF A FUNCTION

## LEARNING OUTCOMES:

At the end of this topic, you are expected to:

1. Define the limit of a function
2. Resolve related problems using the factorization.
3. Solve limit of a function using L'hopital's method.

Assessment Description (Task) (12 marks)
Prove that this function is defined using both factorization and L'hopital's method:
$\mathrm{g}(\mathrm{x})=x 2-4 x-2$,
$\mathrm{x} \rightarrow 2$

## GRADING RUBRICS

|  | REALISTIC OBJECTIVES | POOR | EXCELLENT |
| ---: | :--- | :--- | :--- |
| 1. | Identify the value for x | Not <br> properly <br> identifying <br> the value <br> for x | Identify the value <br> for x |
| 2. | State the formula for the L'hopital's method <br> correctly | Incorrectly <br> stating the <br> formula for <br> the <br> L'hopital's <br> method | State the formula <br> for the L'hopital's <br> method correctly <br> $\mathbf{0}$ marks |


| 3. | Substitute the values of the limit function <br> correctly | Incorrectly <br> substituting <br> the values <br> of the limit <br> function <br> $\mathbf{0}$ mark | Correctly <br> substituting the <br> values of the limit <br> function <br> $\mathbf{4}$ marks |
| ---: | :--- | :--- | :--- |
| 4. | Final answer for the task | Not stating <br> the correct <br> final <br> answer | Correct final <br> answer for the task |

## TOPIC: DIFFERENTIATION

## LEARNING OUTCOMES:

At end of this topic, you should be able to:

1. Use these rules in solving different differentiation problems:
a. Constant Function Rule
b. Linear Function Rule
c. Power Function Rule
d. Rules for Sums and Differences
e. Higher Order Derivatives
f. Product Rule
g. Quotient Rule
h. Chain Rule
2. Differentiate by using First Principles

Assessment Description (Task) (15 marks)
Let $c(x)=1 / 8 x^{2}+3 x+98$ be the total cost function for the commodity.

- Find the average cost and marginal average cost for the commodity.
- From what level of production is Marginal Average Cost $(\mathrm{MAC})=0$
- From what level of production does Marginal Cost (MC) = Average Cost (AC)


## GRADING RUBRICS

|  | REALISTIC OBJECTIVES | POOR | EXCELLENT |
| :--- | :--- | :--- | :--- |
| 1. | Differentiate the function using applicable | Differentiate | Differentiate the |
| rules of differentiation | the function | function using |  |
| without using | applicable rules of |  |  |
|  |  | applicable <br> rules of <br> differentiation |  |
|  |  | differentiation |  |


|  |  | 0 mark | 2 marks |
| :---: | :---: | :---: | :---: |
| 2. | Give the formula for the average cost | State the wrong formula for the average cost 0 mark | States the right formula for the average cost <br> 1 mark |
| 3. | Solve for average cost | Does not solve for average cost 0 mark | Solve for average cost 3 marks |
| 4. | State the formula for marginal cost | Does not state the appropriate formula for marginal cost 0 mark | States the appropriate formula for marginal cost <br> 1 mark |
| 5. | Solve for marginal cost by substituting appropriate values | Does not solve for marginal cost by substituting appropriate vales 0 marks | Solve for marginal cost by substituting appropriate values 2 marks |
| 6. | Solve for marginal average cost to obtain the level of production | Solve for any other <br> function than marginal average cost function 0 marks | Solve for marginal average cost to obtain the level of production 3 marks |


| 7.Equate the values of marginal cost to average <br> cost to obtain the maximum production level <br> of the stated cost function | Solution that <br> does not <br> include <br> equating the <br> values of <br> marginal cost <br> to average <br> cost to obtain | Equate the values <br> of marginal cost to <br> average cost to <br> obtain the <br> maximum <br> production level of <br> the stated cost <br> function <br> the maximum <br> production | $\mathbf{3}$ marks |
| :--- | :--- | :--- | :--- |
| level of the |  |  |  |
| stated cost |  |  |  |
| function |  |  |  |
| $\mathbf{0}$ mark |  |  |  |

## TOPIC: INCREASING AND DECREASING FUNCTIONS

## LEARNING OUTCOMES:

At the end of this topic, you should be able to:

- Interpret increasing and decreasing function
- Solve application problems relating to increasing and decreasing functions

Assessment Description (Task) (10 marks)

Given $Y=4 x^{2}-10 x+100$. Determine whether the function is increasing at $\mathrm{x}=10$ or $\mathrm{x}=5$

## GRADING RUBRIC

|  | Criteria | Poor | Excellent |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Differentiating the function <br> with respect to x | Not <br> differentiating the <br> function with <br> respect to x | Differentiating the <br> function <br> appropriately with <br> respect to x |
| $\mathbf{2}$ | Substituting $\mathrm{x}=10$ and $\mathrm{x}=5$ |  |  |
| into | Not properly <br> substituting the <br> values of x into <br> the differentiated <br> equation, thus <br> arriving at the <br> wrong solution to <br> the problem. <br> 0 mark | mark <br> differentiated <br> equation and <br> solving the |  |
| equation to arrive |  |  |  |
| at a solution. |  |  |  |
| $\mathbf{4}$ marks |  |  |  |


| 3 | Identifying if the function is <br> increasing or decreasing at <br> the point where $\mathrm{x}=10$ and <br> $\mathrm{x}=5$ | Not recognizing if <br> the function is <br> increasing or <br> decreasing where <br> $\mathrm{x}=10$ and $\mathrm{x}=5$ <br> mark | Appropriately <br> Identifying if the <br> function is <br> increasing or <br> decreasing at the <br> point where $\mathrm{x}=10$ <br> and $\mathrm{x}=5$ <br> 2 marks |
| :--- | :--- | :--- | :--- |

## TOPIC: EXTREME VALUES

## LEARNING OUTCOMES:

## At the end of this topic, you should be able to:

1. Determine extreme values
2. Solve application problems relating to extreme values

Assessment Description (Task) (15 marks)
The demand equation for Dangote spaghetti is given as $\mathrm{P}=2 x-0.001 x^{2}$. Find the value of x and the corresponding price that maximizes the revenue

## GRADING RUBRIC

|  | Criteria | (Poor) | (Excellent) |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Using the price <br> equation to derive a <br> revenue function | Not <br> accurately <br> deriving the <br> revenue <br> function from <br> the price <br> equation | Accurately <br> using the price <br> equation to <br> arrive at a <br> revenue <br> function |
| $\mathbf{2}$ | Properly differentiate <br> the derived revenue <br> function. | Inaccurate <br> differentiation <br> of the derived <br> revenue <br> function. <br> 0 mark | differentiate <br> the derived <br> revenue <br> equation. <br> $\mathbf{4}$ marks |
| $\mathbf{3}$ | Solve the <br> differentiated revenue | Not solving <br> the | Solving the <br> differentiated |


| function when <br> equated to zero to get <br> x | differentiated <br> revenue <br> function <br> when equated <br> to zero to get <br> x | revenue <br> function when <br> zero to get x |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{4}$ | Using the value of x <br> to arrive at the <br> maximum price and <br> maximum revenue | Solving for a <br> different <br> value for the <br> maximum <br> price and <br> maximum <br> revenue apart <br> from the <br> value in the <br> third step. | arrive at the <br> maximum <br> price and <br> maximum <br> revenue <br> 3 marks |

Total score: 15 marks

